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A MODEL DRIVEN OPTIMIZATION APPROACH TO DETERMINE TILT ANGLE OF SOLAR COLLECTOR IN INDIA

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ABSTRACT

The solar systems are an intense need to full fill the energy requirement of developing countries like India. Where, thermal and photovoltaic are the two methods to utilize the solar energy directly from sun. In these methods solar equipments (e.g. flat plat collector and Photovoltaic panel) are kept in tilted position for absorbing maximum solar flux. Hence, finding the optimum tilt angle is the problem of optimization. Therefore, in this paper model driven optimization approach such as particle swarm optimization (PSO) estimator has been proposed to find optimum tilt angle and its results are compared with analytical results. A novel cost function has been applied to determine periodical optimum tilt angle. To validate the performance of PSO estimator results, statistical analysis study is carried out. Where, three statistical approaches such as descriptive method, direct method and Altman-Bland methods are adopted. The PSO estimator results are found satisfactory to ANA results at 95% confidence interval under statistical study.

Keywords: Solar panel, PSO, Bland-Altman, Solar Power

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1. INTRODUCTION

India is in deep energy crisis owing to rising prices of conventional energy sources as well as their scarcity. On other hand, the uses of conventional sources of power generations are not only pollute the environment but also fragile the ecological balance. Thus, there is an urgent need to use environment friendly and renewable energy sources such as solar, wind, geothermal etc. Where, solar energy is most valuable, clean and safe source of energy gifted by the nature.

Owing to its location between the tropic of Cancer and the Equator, India has an average annual temperature that ranges from 25° C to -27.5° C. On the other hand, being a tropical country, India has huge potential for solar power generation.

The thermal and photovoltaic conversions are the two methods of direct energy utilization of solar energy. In these two methods most preferable solar equipment's are Flat Plat Collector (FPC) and Photovoltaic Array (PVA) respectively. The solar flux falls on the solar collector depends on the tilt angle from horizontal surface. In other words, the amount of radiation absorbed by solar collector or panels is affected by their orientation and angle of tilt with the horizontal surface. It has been seen that often solar data are given at horizontal surface and also it is not possible to measure the performance of solar equipment's at different tilt angle in large countries like India.

Although, the solar radiation calculation is highly nonlinear, stochastic and site specific, several complex models are available in literature. Further, these models estimate solar radiation in terms of climate parameters such as sunshine hour, relative humidity, cloud layer, maximum temperature etc. [1-3, 7]. The proposed model from different researchers helps to derive the optimum tilt angle at any location around the world from available metrological data on horizontal surface $\beta = 0^{\circ}$ [4-5].

In [1] a number of equations related to mean monthly global solar radiant exposure $\left(E_g\right)$ available in literature have been reviewed. And it has been observed that the original Angstrom type regression equation which relates E_g to clear days radiation at site and average possible sunshine hour ratio are modified by different researchers. These modified models are classified such as linear, polynomial, other (nonlinear, exponential and logarithm term) models. In [7] author has proposed an empirical formula to estimate optimum tilt angle $\left(\beta_{opt}\right)$, hour angle $\left(\omega\right)$ and orientation $\left(\gamma\right)$ of solar panel based on generic surface with respect to position of sun. In [8-11] authors have proposed different empirical formulas to derive optimum tilt angle of solar panel around the world from available metrological data on horizontal surface.

Recently, the soft-computing techniques such as ANN, GA, ANFIS, and PSO etc. becoming popular in solar energy estimation problems of optimization. The ANN to determine β_{opt} has been widely used in solar energy estimation problems [12, 13, and 14]. In [12] the author has taken E_g , ϕ , ρ and E_L as input to ANN model and estimated the optimum tilt angle. Where, Mubiru and Banda [13] have developed ANN based model to predict direct solar irradiance. This proposed ANN model takes sunshine hour, cloud cover, maximum temperature, latitude, longitude as well as altitude of site as input parameters. In [14] author has proposed ANN model to predict direct beam radiation on horizontal surface based on five input parameters such as global solar irradiance, maximum temperature, latitude, longitude and altitude of site. In [15] author has proposed an ANN estimator to predict periodic optimum tilt angle from available input data such as $E_{g(monthly)}$, ϕ , and E_L . Here, ground albedo (ρ) is not taken into account because the variation in ρ is negligible and mostly considered as constant.

The above data driven approach is suitable only if accurate target data to train the ANN is available. But for large country like India due to geographical and astrological variations, accurate and reliable data collection is always not feasible. For reliable data collection it is utmost importance to measure solar radiation data in different part of country. On other hand, the network of radiation measuring stations should be modernized as well as monitored in same data.

In paper [16] GA and Lagrange Multiplier algorithm has been proposed to maximize the photovoltaic panel output. Where, the GA gives initial population at optimal power and then it is feed to Lagrange Multiplier algorithm to find the PV module output power. The [17] presented the β_{out} calculation for fixed flat solar panel based on Genetic Algorithm (GA) and

Simulated-Annealing (SA) methods. The relation between sun incident angle and its radiation intensity on solar cell has been presented. The climate data of different location of Taiwan have been used by GA and SA to obtain the optimum tilt angle β_{ont} .

Till date no work has been reported to obtain β_{ont} using soft computing (model driven approach) in India. The objective of this work is to propose a model driven approach to determine optimum tilt angle (β_{opt}) such that total monthly mean daily solar irradiance (E_{gs}) can be maximized on panel surface. Although the β_{ont} problem can be formulated on daily, weekly, monthly, quarterly, bi-annual and annual basis. In this paper the quarterly, bi-annual and annual model of expected irradiance in (MJ/m²) are presented. The optimum tilt angle of south facing collectors of entire India is calculated on the basis of mean (monthly) global solar irradiance data obtained by Metrological center India [22]. We have proposed a PSO estimator to predict the β_{opt} (periodically). A comparative study of the results obtained by Analytical Analysis (ANA) as well as PSO estimator is carried out. Further, the results of PSO estimators are analyzed based on statistical error tests [17]. In this paper, the results of selected cities of India of different latitude and elevation such as Minicoy (MNC), Thiruvananthapuram (TRV), Port (GOA) Blair Bangalore (BNG), (CHN) Goa Hyderabad (PBL), Chennai (HYD), Visakhapatnam (VSK), Pune (PNE), Mumbai (MMB), Nagpur (NGP), Bhavnagar (BHV), Kolkata (KLK), Ahmadabad (AHM), Bhopal (BHP), (RNC), Varanasi (VNS), Shillong (SHL), Patna (PTN), Jodhpur (JDP), Jaipur (JPR), New Delhi (NDL) are presented.

2. MODELING OF TOTAL SOLAR IRRADIANCE CALCULATOR AT TILTED SURFACE

In general, sensors are placed in a horizontal position to measure direct solar irradiance at Metrological centers. But in solar energy applications to maximize capture of total solar irradiance the panels are normally kept in tilted position. Hence, it becomes essential to derive total solar radiant exposure from available values of monthly mean of daily/hourly global solar irradiance and monthly mean of daily/hourly diffuse irradiance on the tilted panel surface. Sometimes, global solar irradiation data may either not be available or not be desired form. In such case a typical empirical regression (1) suggested by Gopinathan[3] can be considered when data on sunshine hours are available.

$$\frac{E_g}{E_{go}} = a_1 + b_1 \left(\frac{S}{S_{\text{max}}}\right) \tag{1}$$

Where, the a_I , $b_I = f \{ \phi, E_L, S, S_{max} \}$ are regression constants can be obtained by (2-3) [7, 22].

$$a_1 = -0.309 + 0.539\cos\phi - 0.0693E_L + 0.290 \left(\frac{S}{S_{\text{max}}}\right)$$
 -(2)

$$b_{\rm l} = 1.527 + 1.027\cos\phi + 0.0926E_L - 0.359 \left(\frac{S}{S_{\rm max}}\right)$$
 -(3)

The extraterrestrial solar radiation on a horizontal panel for dn^{th} day is given as [7, 9 and 12]

$$E_{go} = \frac{24}{\pi} G_{sc} \left(1 + 0.033 \cos \left(\frac{2\pi \times dn}{365} \right) \right)$$
 -(4)

Moreover, to simplify the calculation of E_{go} , Klein has suggested that the extraterrestrial solar radiation in middle of the each month is nearly equal to the monthly mean value [3]. The hour angle corresponding to sunrise or sunset on the horizontal surface is given by (5)

$$\overline{\omega} = \left[\cos^{-1}\left(\tan\phi\tan\delta\right)\right] \tag{5}$$

Therefore, the corresponding sunshine hour is

$$\overline{S} = \frac{2}{15} \left[\cos^{-1} \left(\tan \phi \tan \delta \right) \right] \tag{6}$$

The angle made by the line joining the centers of the sun and earth with the projection of this line on the equatorial plane, is known as declination angle (δ). There are four models (formulas) are proposed in literature to calculated declination angle, all these formulas are assumption based. All four models are simulated and results are presented in Fig.1.Here could be seen that all four models have no significant difference as far as declination angle calculation is concern.

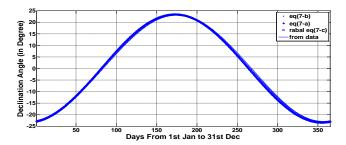


Figure 1 Declination Angle versus day plot

Model-1

$$\delta = 23.45 \sin \left[\frac{2\pi (284 + dn)}{365} \right]$$
 (7-a)

Model-2

$$\delta = \sin^{-1} \left[\sin(23.45) \times \cos \left(\frac{2\pi (dn - 173)}{365.25} \right) \right]$$
 (7-b)

In equation (7-a) and (7-b) dn=1 at 1st Jan of every year [3],[6].

Model-3

Rble's model of inclination angle [5] is given in equation (7-c)

$$\delta = \sin^{-1} \left[-\sin(23.27) \times \cos\left(\frac{2\pi D}{365.25}\right) \right]$$
 (7-c)

Where D- time after winter solstice (i. e D count starts from 22 DEC onwards)

Model-4

This is a data driven model for which data is obtained from Indian Metrological Center Pune (Ref Table-7) [22]

The downward solar radiant energy scatted by the suspended particle, air molecules and the clouds. Many researchers have developed empirical for estimating E_d/E_g ratio for various part

of world [5, 7, 9, and 22]. In this case the prediction of mean monthly daily diffuse irradiance (E_d) on horizontal surface from (8 and 9) is most suitable than other predictors because in fact diffuse components are much larger in India [1-3].

$$\frac{E_d}{E_g} = 0.8677 - 0.7365 \left(\frac{S}{S_{\text{max}}} \right) \tag{8}$$

or
$$\frac{E_d}{E_g} = 1.411 - 1.696 \left(\frac{E_g}{E_{go}} \right)$$
 -(9)

2.1. Solar Irradiance on Tilted Surface

The total solar irradiance E_{gs} on tilted panel is the summation of direct-beam, diffuse and ground reflected radiations on the inclined surface. The E_{gs} can be expressed as (10)

$$E_{\varrho\varsigma} = E_b \Re_b + E_d \Re_d + E_{\varrho} \Re_r \tag{10}$$

Where,

$$E_b = \left(E_g - E_d\right)$$

 \Re_h for sharp south facing $\gamma = 0^{\circ}$ can be expressed as

$$\Re_b = \frac{\omega_s \sin \delta \sin(\phi - \beta) + \cos \delta \cos \omega \cos(\phi - \beta)}{\omega_s \sin \delta \sin \phi + \cos \delta \cos \omega_s \cos \phi}$$
-(11)

$$\mathfrak{R}_d = \frac{(1+\beta)/2}{2} \tag{12}$$

 \Re_r : If ground reflection to be considered as isotropic [9] then

$$\Re d = \frac{\rho(1-\beta)}{2} \tag{13}$$

 ρ : It is the reflection coefficient, generally in India its value in between 0.12 to 0.2 [22].

3. OPTIMUM TILT ANGLE FORECASTING OF PV PANEL USING PSO ESTIMATOR

The Particle Swarm Optimization (PSO) is a stochastic optimization technique based on social behaviour of bee swarming or fish schooling. This method has been proven effective fornon-derivable objective function as well as its implementation wery easy. In PSO each particle adjust its position in searchspace by its own as well as other particle flying experience to find the best global solution for each particle. The performance of each swarm can be improved by defining initial population of each swarm such that each particle closely bounds to the expected domain of feasible region [19], [23]. A realcoded PSO estimator is proposed to find the optimum tiltangle of SOLAR COLLECTOR based on mean monthly global and diffusesolar irradiance during uncertain climate changes at different locations in India. The mathematical model of optimization problem can be described as follow:

$$\min or \, \max f \left\{ X, E_{gs} \right\} \tag{17}$$

Where, X is some equality and Non equality constraints and E_{gs} is the objective function to be maximize.

3.1. Imposed Parametric Constrains

The imposed parametric constraints in this paper for sharp south facing PV array are as follows:

$$dn^{\min} \le dn \le dn^{\max} \Rightarrow 1 \le dn \le 365 \tag{18}$$

$$\beta^{\min} \le \beta \le \beta^{\max} \Rightarrow 0^{\circ} \le \beta \le 90^{\circ} \tag{19}$$

$$\gamma = 0^{\circ}$$
; azimuth angle -(20)

$$\rho = 0.2 \tag{21}$$

In this work the performance of swarms are made better by putting parametric constraints (lower and upper bound constraints) as shown in (18-21), but linear and nonlinear constraints are not taken into account. In PSOeach particle moves about the cost surface with a velocity. The velocities of particles are controlled by ω inertia weight. By decreasing ω global search converges to local search. The particle updates their velocities and position based on the global and local best solution by(22-24). Therefore, the new position of particle can be estimated by following:

$$v_n^{j+1} = \omega v_n^j + C_2 r_1 \left(P_{LB_a}^j - P_n^j \right) + C_1 r_2 \left(P_{GB_a}^j - P_n^j \right)$$
 (22)

$$\omega = \omega^{\max} - \frac{\left(\omega^{\max} - \omega^{\min}\right)}{I_{tor}^{\max}} \times I_{ter}$$
 -(23)

Therefore, the new position of particle can be estimated by following:

$$p_n^{j+1} = p_n^j + v_n^{j+1} -(24)$$

The [20] demonstrated that the particle swarm is only stable if the following conditions are satisfied:

Condition-1:
$$0 < (C_1 + C_2) < 4$$

Condition-2: $\left\{ \frac{(C_1 + C_2)}{2} - 1 \right\} < C_0 < +1$

where, C_0 , C_1 and C_2 are inertia, social attraction and cognitive attraction of the particles respectively. Although, the above conditions ensures the convergence of system but that may not be global minimum. By selecting inertia weight tactfully optimal global solution can be achieved in lesser number of iterations. Here, ω decreases linearly from 0.9 to 0.4 during simulation [19]. The boundary constraint of particle can be managed by either 'Penalize' or 'Reflect' or 'Soft' or 'Absorb' option [20]. In this paper 'Soft' boundary constraint has been taken which sets fitness scores to infinity if particles leave problem bounds. The 'soft' boundary option saves the simulation time since infeasible points are not evaluated.

3.2. PSO Input Parameters

The selected input parameters and their imposed parametric constraints areas follows:

$$X = [\varphi, E_{I}, \rho, S, dn, E_{g}]$$

where, dn is a day of the year (dn=1onJan 1st and dn=365onDec 31st) and ρ =0.2 [22].

3.3. Problem Formulation

The objective of this work is to maximize the E_{gs} over an appropriate period (seasonal, biannual, yearly) by adjusting tilt angle β of solar collector of cities of India. Hence, optimum tilt angle β_{opt} can be obtained by maximizing the cost function $H_{gs}(\beta_i)$ calculated from (10) for each city. Therefore, the fitness function to be optimized is obtained by taking harmonic mean of (10) for each of the latitude. The harmonics mean gives largest weight to smallest item and smallest weight to largest item.

$$F_{\Delta}(X_{i}) = \left[\frac{\sum_{i=1}^{N} \left(\varepsilon_{(\Delta)} \left\{\phi, \beta, \delta, \omega_{s}\right\} + \mu_{(\Delta)} \left\{\beta\right\} + \kappa_{(\Delta)} \left\{\rho, \beta\right\}\right)^{-1}}{\frac{N}{M}}\right]^{-1}$$

$$-(25)$$

with, $\Delta = (C \times M)$ $C \in \{1, 2,23\}$ number of cities under study, $N \in \{12\}$ number of months and $M \in \{1, 2, 4\}$ for annual, bi-annual and seasonal period respectively. Here, ε_{Δ} , κ_{Δ} and μ_{Δ} are the arbitrary functions of corresponding variables.

3.4. Pseudo-code of PSO Implementation

The pseudo code to implantation of Particle Swarm Optimization algorithm is as follows:

Begin

- Select the number of variable to be optimized for each city
- Select number of swarm particles (population size) and generations (maximum no of iterations), as well as set C_1 , C_2 and ω_{\min} and ω_{\max} and terminating criteria.
- Impose the parameter constraints (lower bound, upper bound and other constraints if any).
- Randomly initialize the swarm position $\binom{p_n^j}{n}$ and velocity $\binom{p_n^j}{n}$ of each particle.

Here

• Randomly generate population.

Next

- Impose Constraints: Is satisfied?
 - No
 - o Remove the population and go to next population set.
 - o Go to: Next
 - > Yes
 - o Evaluate fitness function using (25).
 - O Determine P_{LBn}^{j} and P_{GBn}^{j} for each particle of each city.
- Is terminating Criteria reached?
 - > No
 - o Update the swarm position and velocity using (22-24).
 - o Update the inertia weight.
 - \circ Update P_{LBn}^{j} and P_{GBn}^{j} for each particle if its current value is better

- o Go to :Here
- > Yes
 - \circ Compute the best value of $\mathbf{E}_{gs(max)}$ and corresponding independent variable.

End

4. RESULTS AND DISCUSSION

In this paper the seasonal, bi-annual and annual optimum tile angles are predicted for selected cities of India using analytical method and PSO estimator. In particular, the solar radiation data of India are considered by taking average on a monthly basis for period of 11 years (1991-2001) from Indian Meteorology Department (IMD) Pune, India [22]. The exhaustive study of 23 cities has been carried out but due to space limitation the results of six selected cities of different latitude are presented in this paper.

4.1. Comparative study of Analytical and PSO Estimator

Based on analysis presented in section-II several MATLAB program were developed to calculate the maximum total solar irradiance E_{gsmax} for $\gamma=0^{\rm o}$ using (7-10). The optimum tilt angle was calculated by searching for the value at which maximum E_{gsmax} will be obtained. The inclination of solar collector may be adjusted to optimum tilt angle hourly, daily and monthly basis. By shortening the adjustment period the total solar irradiance on solar collector can be increased but these adjustments spends lot of manpower or electrical power in automatic tracking system.

Table 1 Optimum Tilt Angle of Solar Collector on Seasonal Basis using Analytical Method and Pso Estimator

SNL opt	WN _{ANA}	ATANA	SRANA	WN _{PSO}	ATPSO	SR _{PSO}
MNC	36.00	11.00	6.00	35.51	10.65	5.70
TRV	35.00	12.00	5.00	34.63	11.86	4.89
PBL	38.00	15.00	9.00	38.33	15.06	8.83
BNG	40.00	17.00	10.00	39.82	17.08	10.23
CHN	36.00	15.00	8.00	35.82	15.03	7.87
GOA	43.00	19.00	13.00	43.41	18.65	13.11
HYD	46.00	21.00	15.00	45.74	20.65	14.59
VSK	44.00	20.00	14.00	43.57	19.61	14.48
PNE	46.00	21.00	17.00	46.35	21.40	16.93
MMB	44.00	20.00	15.00	44.07	20.29	15.06
NGP	48.00	23.00	19.00	47.72	22.73	18.76
BHV	49.00	24.00	21.00	49.45	24.02	21.29
KLK	46.00	22.00	16.00	46.11	21.73	16.49
AHM	50.00	25.00	21.00	50.07	24.96	21.34
BHP	51.00	25.00	22.00	50.55	25.13	22.29
RNC	49.00	25.00	19.00	48.97	24.73	19.08
VNS	49.00	26.00	21.00	48.93	25.74	21.19
SHL	52.00	26.00	19.00	51.85	26.23	18.91
PTN	49.00	26.00	21.00	49.46	26.16	21.43
JDP	53.00	28.00	24.00	53.40	27.78	23.95
JPR	53.00	27.00	24.00	52.60	27.22	24.26
NDL	53.00	28.00	24.00	52.71	27.93	23.79
Note: Duri	ng summer	in all case	e optimum	tilt angle i	s zero deg	grees.

4.2. Optimum Tilt Angle on Seasonal Basis

In this section simulation result for seasonal adjustment of tilt angle of expected total solar irradiance in (MJ/m²) are presented. The Fig.2 shows the convergence behavior of PSO fitness value for quarter period of the year on seasonal basis. The parameter setting for implementing the proposed PSO algorithm is same as analytical approach. The mean of optimized fitness function reaches to best score 0.0484 at 62 generation. The best individual scores i.e. optimum tilt angle (β_{opt}) among 62 trails are shown for selected cities of India. The simulation result of

ANA and PSO estimator are presented in Table-I, which represents β_{opt} for each season and selected latitude. The total solar irradiance in (MJ/m²) for these approaches to predict the optimum tilt angle is approximately same as shown in Table-2. Form Table-1 and Table-2 it can be observed that PSO approach has better ability to optimize the tilt angle of solar collector to maximize the collection solar energy.

Table 2 Maximum Total Solar Irradiance $E_{gsmax}(Mj/M^2)$ Corresponding to Optimum Tilt Angle of Solar Collector on Seasonal Basis using Analytical Method And Pso Estimator

Egs ^{SNL} max	WNANA	ATANA	SMANA	SRANA	WN _{PSO}	ATPSO	SM _P so	SR _{PSO}
MNC	19.83641	21.38782	16.89667	18.03976	19.83696	21.38811	16.89665	18.03992
TRV	20.93009	22.62209	18.27667	19.27795	20.93041	22.62214	18.27665	19.27797
PBL	20.87194	21.56291	14.49000	15.48524	20.8722	21.56292	14.49000	15.48528
BNG	22.45604	24.39020	19.10333	17.99929	22.45613	24.39022	19.10332	17.99938
CHN	18.05185	23.34558	20.71000	18.28982	18.05191	23.34559	20.70991	18.28985
GOA	24.70772	24.33953	18.36333	18.56207	24.70823	24.33986	18.36331	18.56209
HYD	24.76370	24.95038	20.83333	19.08179	24.76391	24.95074	20.83333	19.08213
VSK	21.28330	22.55773	18.56333	17.35751	21.28378	22.55811	18.56303	17.35789
PNE	23.00623	24.00730	20.20000	18.39556	23.00657	24.00775	20.19983	18.39557
MMB	20.69352	22.88859	18.10000	16.62857	20.69353	22.88880	18.10000	16.62857
NGP	21.73389	23.03411	19.08333	17.59495	21.73410	23.03430	19.08333	17.59505
BHV	24.92165	25.46497	21.71000	19.95153	24.9223	25.46497	21.70998	19.95170
KLK	17.40086	19.53731	17.63333	15.64165	17.40089	19.53746	17.63333	15.64200
AHM	22.91214	24.20319	20.79000	18.51955	22.91216	24.20319	20.78981	18.51976
BHP	23.62239	23.90539	19.55000	18.10153	23.62300	23.90544	19.54999	18.10168
RNC	21.00614	21.73724	17.48000	15.37815	21.00615	21.73741	17.47995	15.37816
VNS	17.95321	21.99334	19.85667	17.72611	17.95322	21.99351	19.85662	17.72617
SHL	21.50543	20.55688	16.96333	15.20201	21.50549	20.55700	16.96333	15.20202
PTN	18.17297	21.91169	19.55000	17.40627	18.17343	21.91175	19.54998	17.40659
JDP	23.57504	23.44017	22.78333	21.17992	23.57552	23.44030	22.78332	21.17992
JPR	21.74466	23.80239	22.84333	19.67433	21.74510	23.80251	22.84332	19.67447
NDL	19.18953	22.26277	22.01333	18.91019	19.18971	22.26278	22.01333	18.91028

4.3. Optimum Tilt Angle on Bi-annual Basis

The aim of this section is to predict the optimum tilt angle of solar collector such that by adjusting it twice a year maximum solar irradiance MJ/m² can be achieved. The bi-annual tilt angle estimation results of PSO are shown in Fig.3. Presently, the PSO estimator is set for 55 generations but in bi-annual adjustment PSO displayed a premature convergence i.e. mean fitness value reaches to best score in less time. The convergence of bi-annual fitness function reaches to best score with in 37 generations. The bi-annual average of daily solar radiant

exposure E_{gsmax} (MJ/m²) for corresponding β_{opt} for different cities is presented in Table-4. Table-3 presents bi-annual optimum tilt angle of solar collector for south direction $(\gamma = 0^{\circ})$.

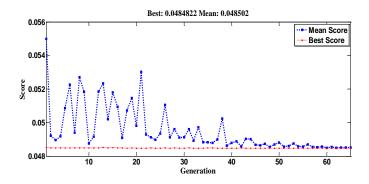


Figure 2 Seasonal Optimum Tilt angle of Selected Cities of India using PSO

4.4. Optimum Tilt Angle on Annual Basis

The convergence behaviour of the fitness value of PSO method for annual basis is shown in Fig.4. The best score of PSO fitness function reaches to 0.04344 at 55 generations. The best individual scores (in degree) among 55 trails are shown for selected cities of India. As shown in Table-5 and Table-6 the proposed PSO approach has better ability to locate the optimum solution then other methods.

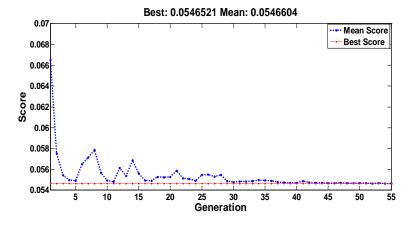


Figure 3 Bi-annual Optimum Tilt angle of Selected Cities of India using PSO

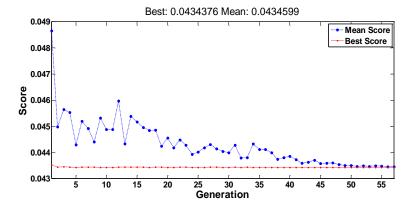


Figure 4 Yearly Optimum Tilt angle of Selected Cities of India using PSO

Table 3 Optimum Tilt Angle of Solar Collector on Bi-Annual Basis Using Analytical Method and Pso Estimator

BYR	COLANA	HOTANA	COL _P so	HOT _P so
MNC	23.00	0.00	22.99	0.00
TRV	23.00	0.00	22.99	2.60E-03
PBL	27.00	0.00	26.66	8.60E-02
BNG	28.00	0.00	28.04	6.60E-05
CHN	24.00	0.00	23.86	9.60E-04
GOA	32.00	1.00	31.68	7.40E-01
HYD	34.00	0.00	33.57	9.28E-04
VSK	32.00	2.00	31.65	1.53
PNE	34.00	3.00	34.00	2.56
MMB	32.00	2.00	31.87	2.21
NGP	35.00	5.00	35.37	4.85
BHV	37.00	6.00	37.16	6.47
KLK	34.00	4.00	33.76	4.45
AHM	38.00	7.00	37.71	6.67
BHP	38.00	8.00	38.32	7.67
RNC	37.00	5.00	37.04	5.11
VNS	36.00	8.00	36.48	7.64
SHL	40.00	7.00	40.17	7.03
PTN	37.00	8.00	37.08	7.90
JDP	41.00	10.00	41.36	9.82
JPR	40.00	9.00	39.95	9.39
NDL	40.00	10.00	39.98	10.03

4.5. Statistical Error Analysis

The statistical methods to assess agreement two quantitative methods such as PSO-ANA of prediction of optimum β have been presented. Where, results obtained by PSO estimator have been compared with analytical results. Here, there are three statistical methods have been adopted such as descriptive analysis, direct comparison method and simple graphical (Bland-Altman) method. In direct comparison method it could be answered that whether one method of β estimation might replace the other with sufficient accuracy. The merits of this approach are that the data will always cluster around a regression line and for comparing two methods it is much more informative. In graphical method difference versus mean of two methods are scattered and it is recommended that 95% of data points should lie within ($\pm 2SD$) of the mean difference. Where, Bland-Altman is a reliably simple graphical parametric approach based on analysis of variance.

Table 4 Maximum Total Solar Irradiance E*gsmax* (Mj/M²) Corresponding to Optimum Tilt Angle of Solar Collector on Bi-Annualbasis using Analytical Method and Pso Estimator

Egsmax	COLANA	HOTANA	COL _{PSO}	HOT _{PSO}
MNC	20.24228	17.43833	20.25462	17.43825
TRV	21.45145	18.75500	21.46491	18.75496
PBL	20.87102	14.93167	20.88790	14.93166
BNG	23.04798	18.46333	23.06854	18.46333
CHN	20.44831	19.44667	20.45985	19.44666
GOA	24.05584	18.31425	24.08164	18.31419
HYD	24.35346	19.75000	24.38119	19.75000
VSK	21.54058	17.79022	21.56152	17.79020
PNE	23.03781	19.05433	23.06354	19.05415

Egsmax	COL _{ANA}	HOT _{ANA}	COL _{PSO}	HOT _{PSO}
MMB	21.42115	17.20370	21.44067	17.20349
NGP	21.94672	18.07562	21.97135	18.07501
BHV	24.66544	20.45251	24.69699	20.45233
KLK	18.15072	16.46724	18.16775	16.46682
AHM	23.08033	19.31221	23.11013	19.31158
ВНР	23.26927	18.46966	23.29900	18.46923
RNC	20.97718	16.20159	21.00206	16.20083
VNS	19.64620	18.48987	19.66862	18.48869
SHL	20.59940	15.90208	20.62798	15.90148
PTN	19.70797	18.17986	19.73142	18.17850
JDP	23.00606	21.52961	23.04057	21.52764
JPR	22.30897	20.82034	22.33835	20.81866
NDL	20.33185	20.09996	20.35808	20.09780

Table 5 Optimum Tilt Angle of Solar Collector on Yearly Basis using Analytical Method and Pso Estimator

eta_{opt}	ANA	PSO	eta_{opt}	ANA	PSO
MNC	11.00	10.51	BHV	25.00	25.50
TRV	11.00	10.94	KLK	22.00	21.73
PBL	17.00	16.60	AHM	26.00	25.83
BNG	17.00	16.57	ВНР	27.00	26.95
CHN	11.00	11.27	RNC	25.00	25.47
GOA	21.00	20.72	VNS	24.00	24.24
HYD	21.00	20.74	SHL	29.00	28.62
VSK	20.00	20.08	PTN	25.00	24.88
PNE	22.00	22.25	JDP	28.00	28.11
MMB	21.00	20.94	JPR	27.00	27.01
NGP	24.00	23.78	NDL	27.00	26.92

4.6. Descriptive Methods

The statistical test results of optimum tilt angle prediction of approaches under study (ANA and PSO) are presented in Table-VII and Table-VIII for annual, bi-annual and seasonal period. Where, it can be observed that there is no significance difference in mean, Standard Deviation (SD) and median of all three methods (ANA and PSO) of β_{opt} prediction of solar collector but this estimation of agreement approach is less effective for larger estimation errors. The covariance and Pearson test result of correlation for two-sided t-test at 95% confidence interval for annual, bi-annual and seasonal period are given in Table-IX and X. The null hypothesis ($H_0: \rho = 0$) is rejected in favor of alternative hypothesis $(H_0: \rho \neq 0)$ at 5% significance level i.e. there is a significance correlation in PSO-ANA estimator result. Moreover, the correlation between ANA and PSO estimator is high [0.999(p < 0.001)]. In this section difference of mean, standard deviation (SD), median and correlation of multivariate analysis are explored to estimate the agreement of two methods. The correlation coefficient (p) only measure the relation between methods but it doesn't grantee the agreement between them. The change in scale of measurement/estimation does not affect the correlation unlike agreement. On the other hand some time data shows poor agreement but produces quite high correlation. Therefore, the correlation coefficient is of no use in practice to compare two methods for their agreement [21].

Table 6 Maximum Total Solar Irradiance <i>Egsmax</i> (Mj/M²) Corresponding to Optimum Tilt Angle of
Solar Collector on Bi-Annual Basis using Analytical Method and Pso Estimator

β_{opt}	ANA	PSO	β_{opt}	ANA	PSO
MNC	18.4607	18.4612	BHV	22.0373	22.0379
TRV	19.7254	19.7254	KLK	16.9679	16.9680
PBL	17.5620	17.5623	AHM	20.6994	20.6995
BNG	20.2919	20.2922	ВНР	20.3931	20.3931
CHN	19.5682	19.5683	RNC	18.1462	18.1466
GOA	20.7172	20.7174	VNS	18.6852	18.6853
HYD	21.4251	21.4253	SHL	17.8010	17.8013
VSK	19.2488	19.2488	PTN	18.5548	18.5548
PNE	20.5440	20.5441	JDP	21.7023	21.7024
MMB	18.9284	18.9284	JPR	21.0576	21.0576
NGP	19.5661	19.5662	NDL	19.7709	19.7709

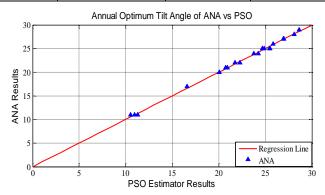


Figure 5 Annual Optimum Tilt angle of ANA versus PSO Estimator Results

4.7. Direct Comparison Method

In direct comparison method it could be answered that whether one method of tilt angle estimation might replace the other with sufficient accuracy. Fig.5, Fig.6 and Fig.7 show the scatter plot between ANA-PSO result with line of equality for annual, bi-annual and seasonal period respectively. The merit of this approach is that the data will always cluster around line of regression which is more informative for comparing two methods.

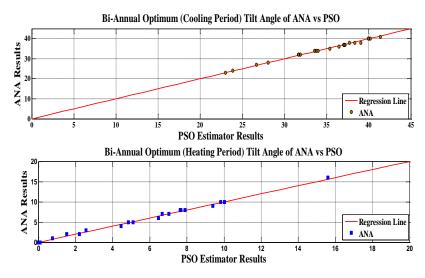


Figure 6 Bi-annual Optimum Tilt angle of ANA versus PSO Estimator Results

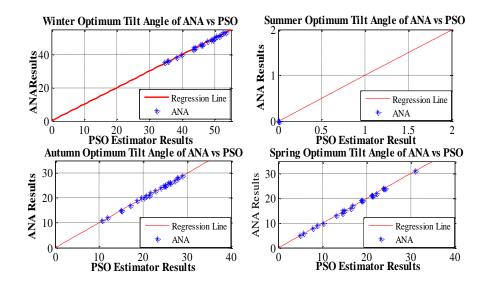


Figure 7 Seasonal Optimum Tilt angle of ANA versus PSO Estimator Results

Table 7 Comparison of Multivariate Analysis Result of Annual β_{opt} Based on Annual Results

D 4	ANNUAL		COL PI	ERIOD	HOT PERIOD	
Parameter	ANA	PSO	ANA	PSO	ANA	PSO
Mean	22.0	21.9	33.9	33.9	4.8	4.8
SD	5.40	5.45	5.50	5.68	4.3	4.3
Median	24.0	23.8	35.0	35.4	5.0	4.8

Table 8 Comparison of Multivariate Analysis Result of Seasonal β_{out}

Parameter	WINTER		AUTUMN		SPRING	
	ANA	PSO	ANA	PSO	ANA	PSO
Mean	46.0	46.1	22.0	21.9	17.1	17.2
SD	5.7	5.8	5.2	5.2	6.5	6.6
Median	48.0	47.7	23.0	22.7	19.0	18.8

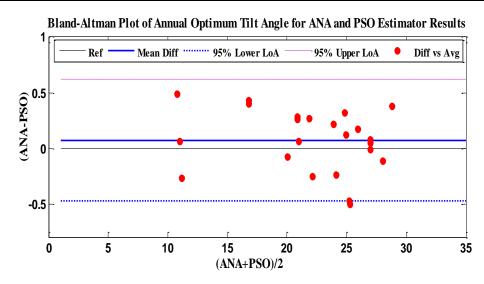


Figure 8 Bland-Altman Plot of Annual Optimum Tilt Angle of ANA versus PSO Estimator Results

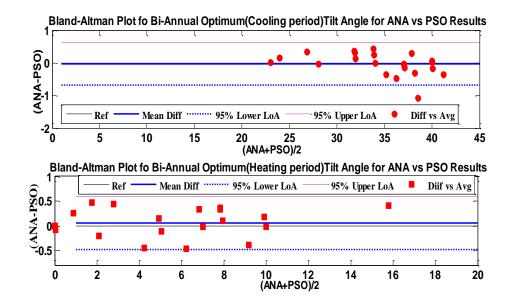


Figure 9 Bland-Altman Plot of Bi-Annual Optimum Tilt Angle of ANA versus PSO Estimator Results

5. CONCLUSION

In this study, evolutionary optimization approach such as PSO estimator that maximizes the total solar irradiance E_{gsmax} on the surface of PV panel has been proposed. The PSO estimator is a model driven approach hence the selection of appropriate model input becomes extremely important. Therefore, the cost function to be optimized using PSO and its constraints are also presented in this work. The PSO estimator predicts the β_{opt} off-line and these results can be used to enhance the energy collection of solar collectors. From the analysis it can be concluded that the PSO estimator is a model driven approach to predict optimum tilt angler (β_{opt}) . This scheme is more effective than data driven approaches such Neural Network, if the target data for training are vague, missing not available. For estimation of seasonal optimum tilt angle, the PSO estimator is more effective, accurate and easy to implement. From statistical study it also can be concluded that the PSO estimator results do not differ by some considered critical difference (at 95% difference of interval), the ANA could be replaced by PSO estimator.

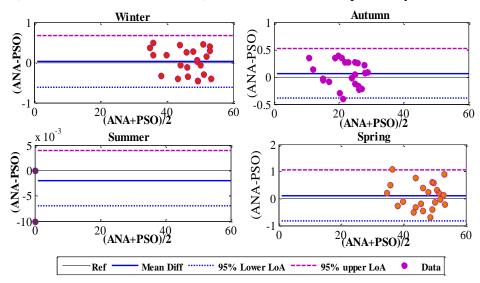


Figure 10 Bland-Altman Plot of Bi-Annual Optimum Tilt Angle of ANA versus PSO Estimator Results

Nomenclature

 E_L Elevation of the site in (meter)

Ego Extraterrestrial solar radiation on horizontal surface for dnth day

 E_{gsmax} Maximum solar radiation collection by solar collector on tilted surface (MJ/m²/day)

 E_g Monthly mean daily global solar irradiance (MJ/m²/day)

 E_d Monthly mean daily diffuse irradiance on horizontal surface (MJ/m²/day) E_b Monthly mean daily beam irradiance on horizontal surface (MJ/m²/day)

S Monthly mean Sunshine hour at horizontal surface

 S_{max} Monthly mean maximum possible Sun shine hour per day at horizontal surface

 G_{SC} Solar constant (4.921 MJ/m²/hr)

MSE Mean square error

SOLAR COLLECTOR Photovoltaic Array

ANA Analytical Analysis/ method

WN Winter

AT Autumn

SM Summer

SR Spring

HOT Heating period of the year

COL Cooling period of the year

SNL Seasonal tilt adjustment

SD Standard Deviation

CI Confidence Interval

LOA Limit of Agreement

Greek Letters

- β Slope or tilt angle of panel surface with respect to the horizontal surface (degree)
- γ Surface azimuth angle (degree)
- δ Earth declination angle (degree)
- ρ Ground reflectance/ albado
- ϕ Latitude of the site in (degree)
- ω Hour angle (degree)
- \mathfrak{R}_{h} Tilt factor for beam radiation
- \mathfrak{R}_{d} Tilt factor for diffuse radiation
- \Re_r Radiation shape factor for surface w.r.t. surrounding ground
- p_n^j Position of nth particle at jth iteration
- v_n^j Velocity of nth particle in jth iteration
- C_1, C_2 Acceleration or learning factors

- r_1, r_2 Independent uniform random number, where $0 \le r_{1,2} \le 1$
- P_{IB}^{j} Best local solution /position of nth until jth iteration
- P_{GB}^{j} Best global solution/position of nth until jth iteration
- ω^{max} Initial parameter weight
- ω^{\min} Final parameter weight
- I_{ter}^{\max} Maximum iteration count
- I_{ter}^{\min} Minimum iteration count
- I_{ter} Current iteration count

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