



Design and Performance Analysis of Proposed Single-Sided Linear Induction Motor used in Elevator

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ABSTRACT

In this paper, single-sided linear induction motor (SLIM) for driving the elevator system is designed. Differing from other motors, SLIM is simple in construction, less expensive, very suitable for linear application which is used from low speed to high speed application. Special machine adjustments and alignments are not necessary in SLIM because mechanical coupling and gears are not required. Thus, SLIM is superior to other linear and rotary motor. The single-sided linear induction motor (SLIM) design, performance equations and design procedure are developed and its performance is predicted by using equivalent circuit model. End effects and edges effects are neglected in this study. The performance of the SLIM for different value of mechanical air-gap are evaluated by using MATLAB. The effect of variation of such parameters on the performance of the machine is discussed.

Keywords: *Linear Induction Motor, Single-Sided Linear Induction Motor (SLIM), Equivalent Circuit Model, Electrical Machine Design, Performance Evaluation*

1. INTRODUCTION:

Linear induction motor (LIM), is basically an advanced types of motor that is use to obtain rectilinear motion instead of rotational motion as in ordinary conventional three phase induction motors. They may be obtained by “cutting” and “unrolling” the rotary induction machines to yield flat, single-sided topologies, where the cage secondary may be used as such or replaced by an aluminium sheet placed between two primaries to make the double-sided LIM. Linear motor potentially have unlimited

applications. Linear induction motors (LIMs) alone have found application in the following general areas: conveyor systems, material handling and storage, people mover (Elevators), liquid metal pumping, machine tool operation, operation of sliding doors and low and high speed trains. There are different types of LIMs, among them, single-sided linear induction motors (SLIMs) are widely used in transportation system. In this paper, single-sided linear induction motor (SLIM) with short primary has been studied for the vertical conveying application because its main characteristic is the linear motion, which takes place without transformation mechanisms, increasing efficiency and the reliability of the system and also eliminating the need for large machine room on the roof. The SLIM has the following advantages comparing with the rotary induction motor (RIM): simple construction, direct electromagnetic thrust propulsion, safety and reliability, precise linear positioning, separate cooling, all electro-mechanical controlled systems used for an induction motors can be adopted for a SLIM without any bigger changes, economical and cheap maintenance.

2. STRUCTURE OF THE SINGLE-SIDED LINEAR INDUCTION MOTOR

The structure diagram of a short primary single-sided linear induction motor (SLIM) is shown in figure 1. The width of primary core, secondary yoke and back iron are different each other. Primary core is symmetrical to the secondary middle line. When the primary windings are excited with the three phase currents, a voltage is induced in the secondary. Thus, three axis forces are produced in the linear induction motor.

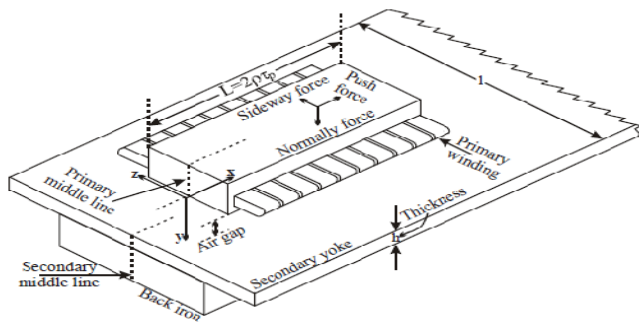


Figure 1. Structure of the single-sided linear induction motor (SLIM)

Number of slot per pole per phase, $q_1=1$
 Aluminum thickness, $d=3\text{mm}$
 Width of stator, $W_{st}=1000\text{mm}$
 Mechanical air gap, $g_m=5\text{mm}$

Continuously, to obtain the target thrust in a Single-Sided Linear Induction Motor, the following equations are used.

$$\text{Synchronous velocity, } v_s = \frac{v_r}{1-s} \tag{1}$$

$$\text{Pole pitch, } \tau = \frac{v_s}{2f} \tag{2}$$

$$\text{Slot pitch, } \lambda = \frac{\tau}{mq_1} \tag{3}$$

$$\text{Length of primary (Stator), } L_s = \tau p \tag{4}$$

$$\tau = 3W_s + 3W_t \tag{5}$$

In this design, the number of slot is 12 and single-layer winding

$$W_t = 1.5W_s \tag{6}$$

And then, get the value tooth width and slot width shown in figure 2.

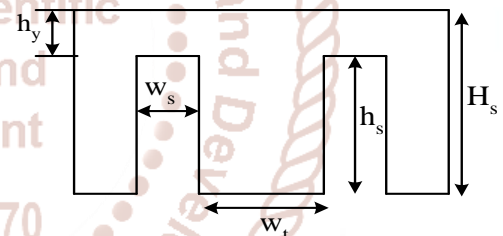


Figure.2 Dimension of Stator Slot

$$\text{Number of turn per phase, } N_1 = N_c p q_1 \tag{7}$$

Where N_1 is the number of turn per phase and set the number of turn per slot N_c to one and increment it by one until the target thrust is obtained.

Now, let assume the product of $\eta \cos \phi$ between 0 and 1 arbitrary.

And find, the value of stator current,

$$I_1 = \frac{F'_s v_r}{3V_{ph} \eta \cos \phi} \tag{8}$$

$$\text{Area of copper wire, } A'_w = \frac{I_1}{J_1} \tag{9}$$

$$\text{Total cross-sectional area of copper wire, } A_{wt} = N_c A'_w \tag{10}$$

3. DESIGN PROCEDURE OF SINGLE-SIDED LINEAR INDUCTION MOTOR

The specifications of SLIM

Target thrust, F'_s : 16000 N
 Rated velocity, v_r : 10 m/s
 Rated Slip, s : 10%
 Rated line voltage, V_1 : 400 V
 Number of phase, m : 3phase
 Number of poles, p : 4poles
 Frequency, f : 50 Hz

Types of winding: Single Layer Winding And, this machine is supposed to be applied in the elevator, achieving vertical transportation with ascending/rising speed v_r and acceleration a up to 10m/s and 2m/s² upwards, respectively. Therefore, the size of the cabin, total weight of cabin and necessary mechanical connection to it, and maximum allowable passenger and the average weight of each passenger are needed to know. All the necessary information are mentioned below

$$\text{Size of cabin, (height} \times \text{length} \times \text{width)}_{\text{cabin}} = 2.5 \times 2 \times 1\text{m}^3$$

Total weight of cabin and bearing, m_{cabin} : 500kg
 Number of passenger in one cabin, n_p : 5
 Average weight of each passenger, $m_{\text{passenger}}$: 75kg

3.1 Design of Primary (Stator)

Stator unit is designed according to the following procedure. First, assign the constant values

Permeability of free space, $\mu_0 = 4\pi \times 10^{-7} \text{H/m}$
 Volume resistivity of Copper, $\rho_w = 19.27 \times 10^{-9} \Omega\text{m}$
 Volume resistivity of Aluminum $\rho_r = 28.85 \times 10^{-9} \Omega\text{m}$
 Stator current density, $J_1 = 6 \text{A/mm}^2$
 Maximum tooth flux density, $B_{\text{imax}} = 1.6 \text{Tesla}$
 Maximum yoke flux density, $B_{\text{ymax}} = 1.3 \text{Tesla}$
 Coil span in electrical radians, $\theta_p = \pi$

$$\text{Cross-sectional area of slot, } A_s = \frac{10}{7} N_c A_w' \quad (11)$$

$$\text{Stator slot height, } h_s = \frac{A_s}{W_s} \quad (12)$$

$$\text{Length of end connection, } L_{ce} = \frac{\theta_p}{180} \tau \quad (13)$$

$$\text{Effective stator width, } W_{est} = W_{st} + L_{ce} \quad (14)$$

Mean length of one turn of the stator winding per phase,

$$L_{wl} = 2W_{est} \quad (15)$$

$$\text{Length of copper wire per phase, } L_w = N_1 L_{wl} \quad (16)$$

$$\text{Total length of copper wire, } T_{Lw} = mL_w \quad (17)$$

After assuming the value of Aluminum thickness of conducting layer, d, the magnetic air gap, g_0 is calculated

$$g_0 = g_m + d \quad (18)$$

And also find the equivalent stator width,

$$W_{seq} = W_{st} + g_0 \quad (19)$$

Gamma for calculating carter's coefficient,

$$\gamma = \frac{4}{\pi} \left[\frac{W_s}{2g_0} \arctan\left(\frac{W_s}{2g_0}\right) - \ln \sqrt{1 + \left(\frac{W_s}{2g_0}\right)^2} \right] \quad (20)$$

$$\text{Carter's coefficient, } k_c = \frac{\lambda}{\lambda - \gamma g_0} \quad (21)$$

$$\text{Effective air gap, } g_e = k_c g_0 \quad (22)$$

$$\text{The goodness factor, } G = \frac{2\mu_0 f \tau^2}{\pi \frac{P_r}{d} g_e} \quad (23)$$

$$\text{Pitch factor, } k_p = \sin \frac{\theta_p}{2} \quad (24)$$

$$\text{Slot angle, } \alpha = \frac{\pi}{mq_1} \quad (25)$$

$$\text{Distribution factor, } k_d = \frac{\sin q_1 \frac{\alpha}{2}}{q_1 \sin \frac{\alpha}{2}} \quad (26)$$

$$\text{Winding factor, } k_w = k_p \times k_d \quad (27)$$

3.2 Equivalent Circuit Model

The equivalent parameters of SLIM can be determined using the per-phase equivalent circuit as shown in figure 3.

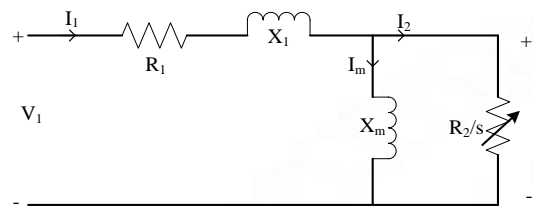


Figure.3 Equivalent Circuit of Linear Induction Motor

$$\text{Per-phase stator resistance, } R_1 = \frac{\rho_w L_w}{A_{wt}} \quad (28)$$

Per-phase slot leakage reactance,

$$X_1 = \frac{2\mu_0 \pi f \left\{ \left[\lambda_s \left(1 + \frac{3}{p} \right) + \lambda_d \right] \frac{W_{st} + \lambda_e L_{ce}}{q_1} \right\} N_1^2}{p} \quad (29)$$

Slot, differential and end connection permeance are

$$\lambda_s = \frac{h_s (1 + 3k_p)}{12W_s} \quad (30)$$

$$\lambda_d = \frac{5 \left(\frac{g_e}{W_s} \right)}{5 + 4 \left(\frac{g_e}{W_s} \right)}$$

$$\lambda_e = 0.3(3k_p - 1)$$

Magnetizing reactance per phase,

$$X_m = \frac{24\mu_0 \pi f W_{seq} k_w N_1^2 \tau}{\pi^2 p g_e} \quad (31)$$

$$\text{Per-phase rotor resistance, } R_2 = \frac{X_m}{G} \quad (32)$$

Using the equivalent circuit parameters from the above equations (28), (29), (31) and (32), and the circuit diagram shown in figure 3, the rated value of impedance can be calculated by

$$Z = R_1 + jX_1 + \frac{j \left(\frac{R_2}{s} X_m \right)}{\frac{R_2}{s} + jX_m} \quad (33)$$

$$\text{Power factor the design motor, } \cos \phi = \frac{\text{Re}(Z)}{|Z|} \quad (34)$$

$$\text{The rated primary RMS phase current, } I_1 = \frac{V_1}{|Z|} \quad (35)$$

Then magnitude of magnetizing current,

$$I_m = \frac{\frac{R_2}{s}}{\sqrt{\left(\frac{R_2}{s}\right)^2 + X_m^2}} \times I_1 \quad (36)$$

Also the magnitude of secondary phase current I_2 can be calculated from

$$I_2 = \frac{X_m}{\sqrt{\left(\frac{R_2}{s}\right)^2 + X_m^2}} \times I_1 \quad (37)$$

The SLIM input active power, $P_i = mV_1I_1 \cos \phi$ (38)

The output power, $P_0 = P_i - mI_1^2R_1 - mI_2^2R_2$ (39)

And then efficiency is calculated by following equation

$$\eta = \frac{P_0}{P_i} \times 100\% \quad (40)$$

The electromagnetic force F_s produced by a machine is given by

$$F_s = \frac{P_0}{v_r} \quad (41)$$

3.3 Required Force Calculation

Resulting magnetomotive force (MMF),

$$\theta_m = \frac{4\sqrt{2}mk_w N_1 I_m}{\pi p} \quad (42)$$

By mean of MMF, the peak value of the normal component of the magnetic flux density is given by

$$B_{gmax} = \frac{\mu_0 \theta_m}{2g_0} \quad (43)$$

Theoretically, the flux in the air gap is sinusoidal because of the sinusoidal voltage source. Thus, the average flux density B_{gavg} can be gained, based on the relation with the peak value of that, i.e

$$B_{gavg} = \frac{2}{\pi} B_{gmax} \quad (44)$$

The yoke of the primary core refer to the section at the top of the core showed in figure 2.

$$h_y = \frac{B_{gavg} \tau}{2B_{gmax}} \quad (45)$$

Making use of L_s , W_{st} and h_y , the volume of the yoke is

$$V_{yoke} = L_s W_{st} h_y \quad (46)$$

In addition, the volume of one tooth of the primary core is

$$V_{tooth} = W_{st} W_t h_s \quad (47)$$

Since the teeth have uniform size, the volume of the total teeth is derived as

$$V_{teeth} = (mpq_1) V_{tooth} \quad (48)$$

Where mpq_1 is the number of slot in a primary core. So, the volume of the iron core of the primary

V_{iron} is $V_{iron} = V_{yoke} + V_{teeth}$ (49)

The weight of the entire iron core, $W_{iron} = \rho_i V_{iron}$ (50)

The weight of copper wire, $W_c = \rho_c A_w T_{lw}$ (51)

The weight of one primary unit W_{stator} , consisting of iron core and copper wire, is easily obtained as

$$W_{stator} = W_{iron} + W_c \quad (52)$$

Number of primary unit, $n_{stator} = \frac{h_{cabin}}{1.2L_s}$ (53)

And then, the **total output thrust** can be calculated as

$$F_t = n_{stator} F_s \quad (54)$$

Now checking the require force by **Newton's Second Law**,

The mass of the whole rising system, $m_t = n_p m_{passenger} + n_{stator} W_{stator} + m_{cabin}$ (55)

The moving resistance of the system D , consists of two components in this specific case, which are

Rolling resistance, $D_r = m_t (c_1 + c_2 v_r)$ (56)

Where c_1 and c_2 are coefficient of correlation, normally defined as 0.01-0.02 N/kg and 0.00015-0.0003 N/kg.

and aerodynamic resistance, $D_a = \frac{1}{2} \rho v_r^2 A$ (57)

Where ρ is the air density 1.205kg/m³ and A is the top or bottom area of cabin 2m².

Total moving resistance is given by

$$D = D_r + D_a \tag{58}$$

Now, making use of Newton’s Second Law of Motion, the force required to be produced by the propulsion system

$$F_s^i = m_t (a + g) + D \tag{59}$$

Where g is acceleration of gravity, 9.8m/s^2 .

Finally, $F_t \geq F_s^i$ becomes a greatly important criterion to decide whether this machine design is satisfied or not.

3.4 Design of Secondary

The single-sided linear induction motor secondary (rotor) design contains conduction layer design and reaction plate design, it is illustrated in figure 4.

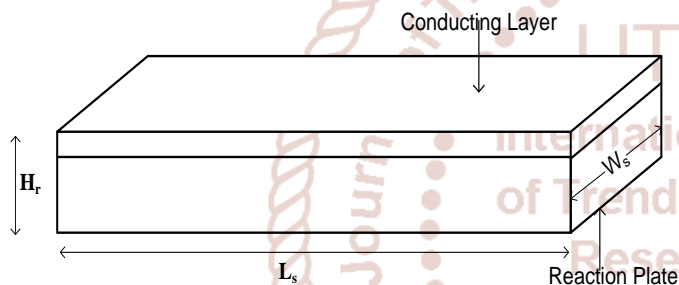


Figure.4 Dimension of Secondary (Rotor)

The secondary reaction plate design which can consist of either solid or laminated design. To improve performance, the reaction plate is coated with conduction sheet of either aluminium or copper. For standard operating, the reaction plate should not be any less than 6mm thick and the attached conducting sheet should not be any less than 3mm thick. The best thrust per size ratio is obtained.

$$W_{se} = W_{st} + \frac{2\tau}{\pi} \tag{60}$$

Where W_{se} is width of secondary and W_{st} is width of primary

4. DESIGN CALCULATION RESULTS OF SLIM

According to the design procedure in section 3, design calculation result of single-sided linear induction motor are mentioned with the following tables.

Table1. Design of Primary

	Parameters	Symbol	Values	Unit
Stator winding design	Copper wire size	-	1	SWG
	Diameter of wire	-	7.62	mm
Stator core design	Length of stator	L_s	450	mm
	Width of stator	W_{st}	1000	mm
	Slot width	W_s	14.7	mm
	Tooth width	W_t	22	mm
	Slot height	h_s	32.73	mm
	Yoke height	h_y	12.51	mm

Table2. Design of Secondary

Parameters	Symbol	Values	Unit
Length of secondary	L_{se}		
Width of secondary	W_{se}	1100	mm
Thick of conducting layer	d	3	mm
Thick of reaction plate		6	mm

The length of the secondary will be as long as the motion length. So, the length of secondary is not illustrated in table 2.

The design data sheet of electrical parameters of SLIM is presented in table 3. In the electrical parameters design, neglect the core losses.

Table3. Design Output of Electrical Parameters

Parameters	Symbol	Values	Unit
Per-phase stator resistance	R_1	0.00356	Ω
Per-phase stator slot leakage reactance	X_1	0.1371	Ω
Per-phase magnetizing reactance	X_m	1.1795	Ω
Per-phase rotor resistance	R_2	0.2055	Ω
Supply current	I_1	201.605	A
Input active power	P_i	62.854	kW
Output power	P_o	56.211	kW
Efficiency	η	0.89	%
Power factor	$\cos \phi$	0.45	-

This motor is designed to move the total mass of 1643.5kg. It is needed 19.54kN output thrust with the rated velocity 10m/s. The outputs for the design motor are tabulated below table 4.

Table4. Design Output of SLIM

Parameters	Symbol	Values	Unit
Total output thrust	F_t	22.5	kN
Velocity	v_r	10	m/s

5. PERFORMANCE CURVES OF SLIM

The input data used for SLIM design in MATLAB program was given in above section(3) along with the slot geometry. The performance characteristics of the SLIM are shown in following figures.

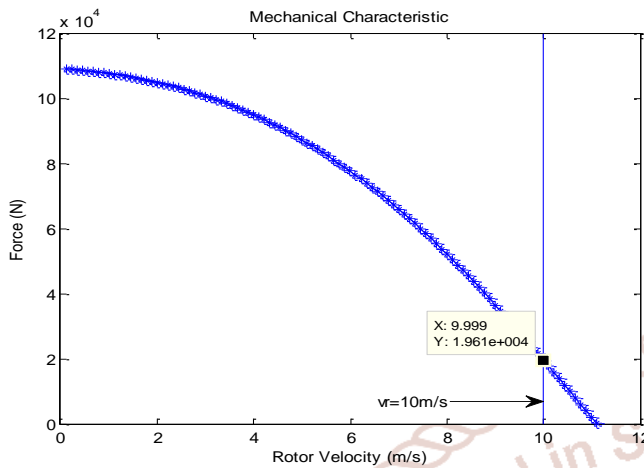


Fig.5 Thrust (Force) F_s' versus rotor velocity v_r of SLIM stator unit at a rated slip of 10%, a desired rotor velocity of 10m/s, a target thrust of 16kN and final thrust of 19.61kN

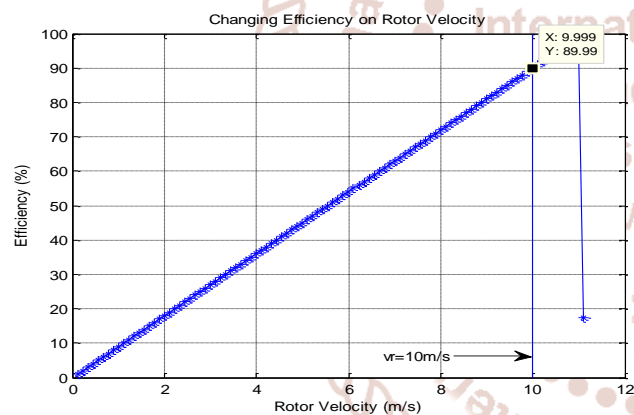


Fig.6 Efficiency η versus rotor velocity v_r of SLIM stator unit at a rated slip of 10%, a desired rotor velocity of 10m/s, a target thrust of 16kN

6. PERFORMANCE EVALUATION OF SLIM BY CHANGING PARAMETER

The performance of the SLIM based on this particular design is evaluated by varying certain parameter like the mechanical air gap. Based on this evaluation, the best possible value for this parameter is selected as shown in the following sections.

6.1 Effect of Mechanical Air Gap on Performance

The length of the air gap plays the most critical role determining the characteristics of the machine. A large air gap requires a large magnetizing current and results in a smaller power factor. In the case of SLIM, exit-end zone losses increase with a larger air gap.

Also, output thrust and efficiency decrease when the design incorporates a large air gap. The goodness factor is inversely proportional to the air gap. Thus, it is clear that the air gap should be as small as is mechanically possible. The different performance values with varying air gap are shown in figure 7 and 8. When the air gap is changed, keeping all other parameters fixed, the efficiency slightly decreases with increasing air gap and the output thrust decreases as the air gap is increased.

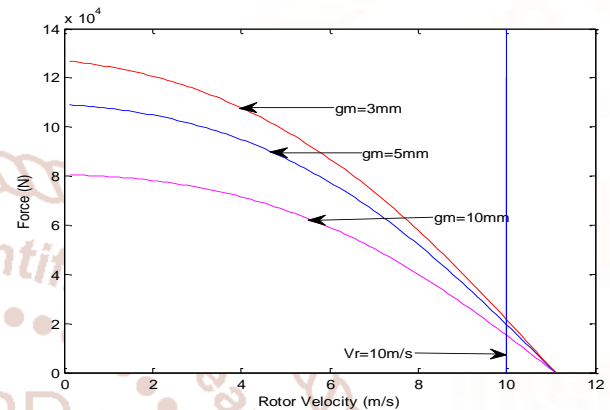


Fig.7 Effect of mechanical air gap on thrust of SLIM at a rated slip of 10% and a target thrust of 16kN

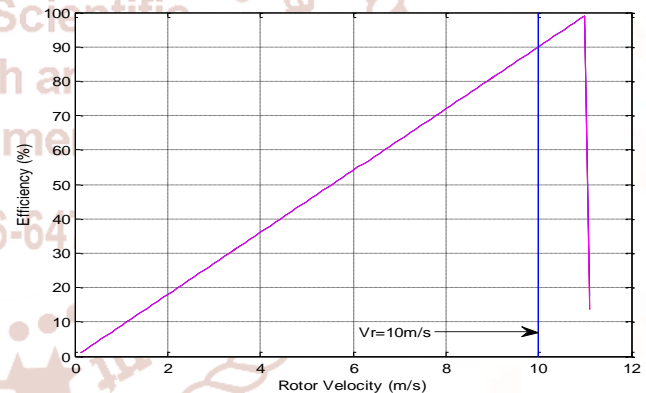


Fig.8 Effect of mechanical air gap on efficiency of SLIM at a rated slip of 10% and a target thrust of 16kN

Table5. Air Gap Effect on Thrust (Force) and Efficiency

Air gap(mm)	Thrust(kN)	Efficiency(%)
3	21.66	90
5	19.16	89.99
10	15.18	89.89

7. CONCLUSION

In this paper, the equivalent circuit has been derived to analyze the performance of the short primary SLIM. So, from the parametric analysis it can be concluded that the input parameter like the length of

the mechanical air gap plays a very important role in the performance parameters, thrust and efficiency. As the length of the mechanical air gap of the machine increases thrust and efficiency of the machine decrease. Hence, based on the target values of rotor velocity and thrust, this parameter should be chosen which gives the best possible thrust closest to the target value at a required frequency.

8. ACKNOWLEDGMENTS

The author is deeply grateful to Dr. Nan Win Aung, my dissertation supervisor and Daw May Nwe Ye Tun, my co-supervisor. The author also thanks to all teachers at Technological University (Thanlyin) and all who provided her with necessary assistance for this paper. The author wishes to express her guidance to all persons who helped directly or indirectly towards the successful completion of paper. Finally, the author wishes to express her special thanks to her parents for their support and encouragement to attain her destination without any trouble.

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